

1. $-(-a^4) \times \left(\frac{2}{a}\right)^3$ 을 간단히 하면?

- ① $-6a$ ② $6a$ ③ $8a$ ④ $-8a$ ⑤ $4a$

해설

$$-(-a^4) \times \left(\frac{2}{a}\right)^3 = a^4 \times \frac{8}{a^3} = 8a$$

2. 다음 중 옳은 것은?

- ① $x \times (-3x^2) = -3x^2$ ② $-2x \times 2y = -4x$
③ $\frac{1}{3}x^2y \times (-9xy^2) = -3x^3y^2$ ④ $(2x)^2 \times (x)^2 = 4x^5$
⑤ $\frac{3}{2}xyz^2 \times \frac{2}{3}x^2y^2z = x^3y^3z^3$

해설

- ① $-3x^3$
② $-4xy$
③ $-3x^3y^3$
④ $4x^4$

3. $\frac{2}{3}ab^3 \times 3a^2b$ 를 간단히 한 것으로 옳은 것은?

- ① $2a^2b^4$ ② $3a^3b^4$ ③ $2a^3b^4$ ④ $3a^3b^3$ ⑤ $2a^3b^5$

해설

$\frac{2}{3}ab^3 \times 3a^2b$ 를 간단히 하면 $\frac{2}{3}ab^3 \times 3a^2b = 2 \times ab^3 \times a^2b = 2a^3b^4$ 이다.

4. 다음 □ 안에 들어갈 알맞은 수를 차례로 나열한 것은?

$$\left(\frac{2}{a}\right)^3 \times \left(\frac{3a}{b}\right)^2 = \frac{8}{a^3} \times \frac{9a^2}{b^2} = \frac{72}{ab^2}$$

① 3, 2, 1, 3 ② 3, 2, 1, 2 ③ 3, 2, 2, 2

④ 4, 2, 1, 2 ⑤ 4, 1, 1, 2

해설

$$\left(\frac{2}{a}\right)^3 \times \left(\frac{3a}{b}\right)^2 = \frac{8}{a^3} \times \frac{9a^2}{b^2} = \frac{72}{ab^2}$$

5. $(2ab^2)^2 \times \left(\frac{a^2}{2b^3}\right)^4 \times \left(\frac{2b^4}{a^5}\right)^2$ 을 간단히 하면?

- ① 1 ② a ③ b ④ $\frac{b}{a}$ ⑤ $\frac{1}{b}$

해설

$$\begin{aligned}(2ab^2)^2 &\times \left(\frac{a^2}{2b^3}\right)^4 \times \left(\frac{2b^4}{a^5}\right)^2 \\&= 4a^2b^4 \times \frac{a^8}{16b^{12}} \times \frac{4b^8}{a^{10}} = a^0b^0 = 1\end{aligned}$$

6. $ax^2y^3 \times (-xy)^b = -5x^cy^6$ 일 때, 자연수 a, b, c 에 대하여 각각의 값은?

- ① $a = 1, b = 2, c = 3$ ② $a = 3, b = 4, c = 3$
③ $a = 5, b = 2, c = 3$ ④ $\textcircled{a} a = 5, b = 3, c = 5$
⑤ $a = 4, b = 5, c = 3$

해설

$$\begin{aligned} & ax^2y^3 \times (-xy)^b \\ &= a \times (-1)^b \times x^2 \times x^b \times y^3 \times y^b \\ &= -5x^cy^6 \\ & a \times (-1)^b = -5, 2 + b = c, 3 + b = 6 \text{ } \circ \text{]므로} \\ & \therefore a = 5, b = 3, c = 5 \end{aligned}$$

7. $axy^2 \times (xy)^b = -3x^c y^5$ 을 때, a, b, c 의 값은?

- ① $a = -1, b = -2, c = 3$ ② $a = -3, b = -4, c = 3$
③ $a = 4, b = -2, c = 3$ ④ $a = 3, b = 3, c = 4$
⑤ $a = -3, b = 3, c = 4$

해설

$$\begin{aligned} axy^2 \times (xy)^b &= -3x^c y^5 \\ ax^{(1+b)} y^{(2+b)} &= -3x^c y^5 \text{ 이므로} \\ a = -3, 1+b &= c, 2+b = 5 \\ \therefore a = -3, b &= 3, c = 4 \end{aligned}$$

- | | |
|--|---|
| <input type="radio"/> A. $(-ab)^3 \times (-3b)$ | <input type="radio"/> B. $(-3ab) \times (-2b)$ |
| <input checked="" type="radio"/> C. $(-2ab)^3 \times 4b$ | <input type="radio"/> D. $\left(-\frac{1}{3}ab\right)^2 \times (3ab)^3$ |

- (㉠) $-24ab$
- (㉡) $-20xy^2$
- (㉢) $-32a^3b^4$
- (㉣) $3a^5b^5$

9. 다음 중 계수가 가장 큰 것과 가장 작은 것을 차례로 나열하면?

$\textcircled{\text{A}} \quad 3a \times 2b$	$\textcircled{\text{B}} \quad \left(\frac{1}{4}ab\right)^2 \times (2ab)^3$
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$\textcircled{\text{C}} \quad (-ab)^3 \times 2b$	$\textcircled{\text{D}} \quad (-4x) \times (-3y)^2$
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해설

$\textcircled{\text{A}} \quad 6ab$

$\textcircled{\text{B}} \quad \frac{a^5b^5}{2}$

$\textcircled{\text{C}} \quad -2a^3b^4$

$\textcircled{\text{D}} \quad -36xy^2$

② ①, ④

③ ①, ⑤

④ ②, ③

⑤ ③, ②

10. $(-b^2)^2 \times \left(\frac{3}{b}\right)^3$ 을 간단히 하면?

- ① $3b$ ② $9b$ ③ $12b$ ④ $24b$ ⑤ $27b$

해설

$$(-b^2)^2 \times \left(\frac{3}{b}\right)^3 = b^4 \times \frac{27}{b^3} = 27b$$

11. $-2x^4y^3 \div x^2y \times (-2xy)^2 = Ax^By^C$ 일 때 $A + B + C$ 의 값을 구하면?

- ① 0 ② 2 ③ 4 ④ 8 ⑤ 16

해설

$$\begin{aligned}-2x^4y^3 &\div x^2y \times (-2xy)^2 \\&= -2x^4y^3 \times \frac{1}{x^2y} \times 4x^2y^2 \\&= -8x^4y^4 = Ax^By^C\end{aligned}$$

$$A = -8, B = 4, C = 4 \text{ } \therefore A + B + C = 0$$

12. 다음 중 옳지 않은 것은?

- ① $x \times (-2x^2) = -2x^3$ ② $-3x \times 4y = -12xy$
③ $\frac{2}{3}x^2y \times (-6xy^3) = -4x^3y^4$ ④ $(3x)^2 \times (2x)^2 = 12x^4$
⑤ $\frac{3}{2}xyz^2 \times \frac{2}{3}x^2yz = x^3y^2z^3$

해설

④ $(3x)^2 \times (2x)^2 = 9x^2 \times 4x^2 = 36x^4$

13. 다음 중 옳은 것을 고르면?

- ① $(-a^2)^2 \times (2b)^3 = -4a^4b^3$ ② $(-3y)^2 \times (-xy)^3 = -3x^3y^5$
③ $(-xy)^2 \times 2xy = 2x^2y^2$ ④ $\left(-\frac{1}{a}\right)^2 \times \left(\frac{2a}{b}\right)^3 = \frac{4}{b^3}$
⑤ $a^2 \times (-2b)^2 \times a^3 = 4a^5b^2$

해설

- ① $(-a^2)^2 \times (2b)^3 = 8a^4b^3$
② $(-3y)^2 \times (-xy)^3 = -9x^3y^5$
③ $(-xy)^2 \times 2xy = 2x^3y^3$
④ $\left(-\frac{1}{a}\right)^2 \times \left(\frac{2a}{b}\right)^3 = \frac{8a}{b^3}$

14. $(3ab)^2 \times \left(\frac{a^2}{b^2}\right)^4 \times \left(\frac{b^4}{a^3}\right)^2$ 을 간단히 하면?

- ① $3ab$ ② a^2 ③ a^4b^2 ④ $9a^2b^2$ ⑤ $9a^4b^2$

해설

$$(3ab)^2 \times \left(\frac{a^2}{b^2}\right)^4 \times \left(\frac{b^4}{a^3}\right)^2 \\ = 9a^2b^2 \times \frac{a^8}{b^8} \times \frac{b^8}{a^6} = 9a^4b^2$$

15. $(-2a^2)^2 \times (-3a^5) \times \frac{3}{4}a^3$ 을 간단히 하면?

① $-9a^{14}$

④ $\frac{9}{2}a^9$

② $-9a^{12}$

⑤ $9a^{12}$

③ $-\frac{9}{2}a^9$

해설

$$(-2a^2)^2 \times (-3a^5) \times \frac{3}{4}a^3$$

$$= 4a^4 \times (-3a^5) \times \frac{3}{4}a^3 = -9a^{12}$$

16. $(-a^2)^2 \times (2a^3) \times \frac{5}{2}a^4$ 을 간단히 하면?

- ① $-5a^{14}$ ② $-5a^9$ ③ $-\frac{3}{2}a^9$
④ $5a^{10}$ ⑤ $\textcircled{5} 5a^{11}$

해설

$$(-a^2)^2 \times (2a^3) \times \frac{5}{2}a^4 = a^4 \times 2a^3 \times \frac{5}{2}a^4 = 5a^{11} \text{이다.}$$

17. 단항식 $x \times (x^3)^4 \times x^3$ 을 계산하면?

- ① x^{14} ② x^{15} ③ x^{16} ④ x^{17} ⑤ x^{18}

해설

$$x \times (x^3)^4 \times x^3 = x^{1+12+3} = x^{16}$$

18. $2 \times 2^{\square} \times 2^3 = 64$ 일 때, $\boxed{\quad}$ 안의 수는?

- ① 1 ② 2 ③ 3 ④ 4 ⑤ 5

해설

$$2^{\square} \times 2^4 = 64 = 2^6$$

$$\square + 4 = 6 \quad \therefore \quad \square = 2$$

19. $2^5 \times 3^3 \times 2^3 \times 3^5$ 을 간단히 하면?

- Ⓐ ① 6^8 Ⓑ ② 6^5 Ⓒ ③ 6^{15} Ⓓ ④ 23^{15} Ⓕ ⑤ 23^8

해설

$$2^5 \times 3^3 \times 2^3 \times 3^5 = 2^8 \times 3^8 = 6^8$$

20. $10 \times 12 \times 14 \times 16 \times 18 \times 20 = 2^a \times 3^b \times 5^c \times 7$ 을 간단히 하였을 때
 $a + b + c$ 의 값은?

- ① 14 ② 15 ③ 16 ④ 17 ⑤ 18

해설

$$\begin{aligned}10 \times 12 \times 14 \times 16 \times 18 \times 20 \\&= 2 \times 5 \times 2^2 \times 3 \times 2 \times 7 \times 2^4 \times 2 \times 3^2 \times 2^2 \times 5 \\&= 2^{11} \times 3^3 \times 5^2 \times 7 \\&= 2^a \times 3^b \times 5^c \times 7 \\a = 11, b = 3, c = 2 \\∴ a + b + c = 11 + 3 + 2 = 16\end{aligned}$$

21. 다음 식을 간단히 한 것 중 옳지 않은 것은?

① $(-x^2y^3)^2 \div \left(\frac{1}{3}xy\right)^2 = 9x^2y^4$

② $(-2x^2y)^3 \times (2xy)^2 = 32x^8y^5$

③ $-4(x^2)^2 \div 2x^4 = -2$

④ $2x^3 \times (-3x^2) = -6x^5$

⑤ $16x^2y \div 2xy \times 4x = 32x^2$

해설

$$\begin{aligned} ② (-2x^2y)^3 \times (2xy)^2 &= -8x^6y^3 \times 4x^2y^2 \\ &= -32x^8y^5 \end{aligned}$$

22. $2a^2b^3 \div (2ab)^3$ 을 간단히 한 것으로 옳은 것은?

① $\frac{1}{4a}$

② $\frac{1}{4ab}$

③ $\frac{1}{4a^2b}$

해설

$$2a^2b^3 \div (2ab)^3 = 2a^2b^3 \div 8a^3b^3 = \frac{1}{4a}$$

23. $(a^2b^x)^3 \div a^y b^3 = a^5 b^9$ 일 때, $x + y$ 의 값은?

- ① 2 ② 3 ③ 4 ④ 5 ⑤ 6

해설

$$(a^2b^x)^3 \div a^y b^3 = a^5 b^9$$

$$a^{6-y} b^{3x-3} = a^5 b^9$$

$$6 - y = 5 \quad \therefore y = 1$$

$$3x - 3 = 9 \quad \therefore x = 4$$

$$\therefore x + y = 5$$

24. $42x^3y^2 \div 12xy^3 \div \frac{7x}{y}$ 를 간단히 하면?

- ① $\frac{1}{2}x$ ② $3x^2$ ③ $7xy$ ④ $\frac{2x}{3}$ ⑤ x^2y^3

해설

$$(\text{준식}) = 42x^3y^2 \times \frac{1}{12xy^3} \times \frac{y}{7x} = \frac{x}{2}$$

25. $14x^2 \div (-7x) \div (-2x)$ 를 계산하면?

- ① 1 ② 2 ③ 3 ④ 4 ⑤ 5

해설

$$14x^2 \div (-7x) \div (-2x) = 1$$

26. 다음 중 계산 결과가 옳은 것을 모두 고르면?

$$\textcircled{1} \quad 6a^3 \div 2ab = \frac{3a^3}{b}$$

$$\textcircled{3} \quad (x^2)^3 \div (-2x^2)^3 = -\frac{1}{6}$$

$$\textcircled{5} \quad (-x^2y)^3 \div (2xy^3) = -\frac{x^5}{3}$$

$$\textcircled{2} \quad \frac{1}{3}x^3y \div \frac{1}{9}x^2y^2 = \frac{3x}{y}$$

$$\textcircled{4} \quad (-x^2y)^2 \div \left(\frac{1}{3}xy\right) = 3x^3y$$

해설

$$\textcircled{1} \quad 6a^3 \div 2ab = \frac{3a^2}{b}$$

$$\textcircled{3} \quad (x^2)^3 \div (-2x^2)^3 = -\frac{1}{8}$$

$$\textcircled{5} \quad (-x^2y)^3 \div (2xy^3) = -\frac{x^5}{2}$$

27. 다음 식을 간단히 하면?

$$xy \div \{(-xy)^2 \div x^2y^3\}$$

- ① $\frac{1}{2}$ ② xy ③ xy^2 ④ x^2y ⑤ x^2y^2

해설

$$\begin{aligned} xy \div \{(-xy)^2 \div x^2y^3\} &= xy \div \left(\frac{x^2y^2}{x^2y^3} \right) \\ &= xy \times y = xy^2 \end{aligned}$$

28. $-(-3x^2y^{\square})^4 \div (-\square x^{\square}y^2)^2 = -x^2y^8$ ⇒ 성립할 때, \square 안에 들어갈 수의 합은?

- ① 10 ② 12 ③ 15 ④ 16 ⑤ 18

해설

$$-(-3x^2y^{\square})^4 \div (-\square x^{\square}y^2)^2 = \frac{-(3^4 x^8 y^{4\square})}{\square^2 x^{2\square} y^4}$$

$$= -x^2y^8$$

이므로 \square 안에 들어갈 수는 각각 3, 9, 3이다.
따라서 합은 15이다.

29. $(3x^2y^{\square})^2 \div (\square x^{\square}y^2) = x^2y^4$ 이 성립할 때, \square 안에 들어갈 수를 차례로 나열하면?

- ① 3, 5, 2 ② 4, 8, 2 ③ 3, 9, 2
④ 5, 8, 2 ⑤ 5, 9, 2

해설

$$(3x^2y^{\square})^2 \div (\square x^{\square}y^2) = \left(\frac{3^2 x^4 y^{2\square}}{\square x^{\square} y^2} \right) = x^2y^4$$

이므로 \square 안에는 3, 9, 2 가 들어간다.

30. $(2xy^a)^3 \div (x^c y^2)^3 = \frac{b}{x^3 y^3}$ 가 성립할 때, $a + b - c$ 의 값은?

- ① 5 ② 6 ③ 7 ④ 8 ⑤ 9

해설

$$(2xy^a)^3 \div (x^c y^2)^3 = \frac{(2^3 x^3 y^{3a})}{x^{3c} y^6} = \frac{b}{x^3 y^3} \text{이므로}$$

$$a = 1, b = 8, c = 2$$

$$\therefore a + b - c = 7$$

31. $18a^3b^3 \div 3a^2b \times 2b$ 를 간단히 하면?

- ① $3ab$ ② $6ab^2$ ③ $12ab^2$ ④ $3ab^3$ ⑤ $12ab^3$

해설

$$18a^3b^3 \times \frac{1}{3a^2b} \times 2b = 12ab^3$$

32. $8a^2b^2 \times 2a^2b \div (-2a^2b)^3 \times 3a^4b^2$ 을 간단히 하면?

- ① $-3a^2b^2$ ② $3a^2b^2$ ③ $-6a^2b^2$
④ $6a^2b^2$ ⑤ $-8a^2b^2$

해설

$$\begin{aligned} & 8a^2b^2 \times 2a^2b \div (-2a^2b)^3 \times 3a^4b^2 \\ &= 8a^2b^2 \times 2a^2b \times \left(-\frac{1}{8a^6b^3}\right) \times 3a^4b^2 \\ &= -6a^2b^2 \end{aligned}$$

33. 다음 식을 간단히 하면?

$$56a^2b \div (2a^2b^2)^3 \times 3a^5$$

- ① $\frac{21a}{b^5}$ ② $\frac{21a^2}{b^5}$ ③ $\frac{28a}{b^5}$ ④ $\frac{28}{b^3}$ ⑤ $\frac{84a}{b^5}$

해설

$$56a^2b \div (2a^2b^2)^3 \times 3a^5 = 56a^2b \times \frac{1}{8a^6b^6} \times 3a^5 = \frac{21a}{b^5}$$

34. 다음 중 계산 결과가 옳지 않은 것은?

$$\textcircled{1} \quad (-2xy^2) \times (3x)^2 \div (6y)^2 = -\frac{x^3}{2}$$

$$\textcircled{2} \quad 14a^2 \div (-2b^2)^2 \times (3ab^2)^2 = -28a^4$$

$$\textcircled{3} \quad \left(\frac{2}{3}a^2\right)^2 \times (3b^2)^2 \div (4ab^2)^2 = \frac{a^2}{4}$$

$$\textcircled{4} \quad (10a)^2 \times (-ab^2)^2 \div \left(-\frac{1}{3}ab^2\right)^2 = 900a^2$$

$$\textcircled{5} \quad (-4x^2y) \div \left(-\frac{2}{3}y^2\right) \times (2xy^2)^3 = 48x^5y^5$$

해설

$$14a^2 \div (-2b^2)^2 \times (3ab^2)^2$$

$$= 14a^2 \div 4b^4 \times 9a^2b^4$$

$$= \frac{63a^4}{2}$$

35. 다음 $\boxed{\quad}$ 안에 들어갈 알맞은 수를 차례로 나열한 것은?

$$(xy^2)^{\square} \div (-xy^3) \times (\boxed{\quad}x^2y) = (-7x^3y^{\square})$$

- ① 2, 4, 3 ② 3, 4, 3 ③ 2, 7, 2
④ 2, 5, 3 ⑤ 3, 4, 5

해설

$$(xy^2)^2 \div (-xy^3) \times (7x^2y) = (-7x^3y^2)$$

36. $(a^2b^4)^3 \times (a^3b^2) \div (ab^3)^2$ 을 간단히 하면?

① a^6b^{10}

② $\textcircled{2} a^7b^8$

③ $a^{10}b^{16}$

④ $a^{11}b^5$

⑤ $a^{15}b^8$

해설

$$a^6b^{12} \times a^3b^2 \div a^2b^6 = a^7b^8$$

37. 다음 식을 계산하면?

$$\frac{3}{7}x^4 \times \left(\frac{7}{12}x^3y \right) \div \left(-\frac{1}{4}xy^2 \right)$$

- Ⓐ $-\frac{x^6}{y}$ Ⓑ $-\frac{x^4}{y^2}$ Ⓒ $\frac{x^4}{y^2}$ Ⓓ $\frac{x^6}{y}$ Ⓕ $\frac{x^6}{y^2}$

해설

$$\begin{aligned} & \frac{3}{7}x^4 \times \left(\frac{7}{12}x^3y \right) \div \left(-\frac{1}{4}xy^2 \right) \\ &= \frac{3}{7}x^4 \times \frac{7}{12}x^3y \times \left(-\frac{4}{xy^2} \right) \\ &= -\frac{x^6}{y} \end{aligned}$$

38. 다음 중 옳지 않은 것은?

① $\left(\frac{2b}{3}\right)^3 = \frac{8b^3}{27}$

② $20a^3 \div 5a^2b = \frac{4a}{b}$

③ $3(ab^2c^4)^2 = 3a^2b^4c^6$

④ $(x^3)^4 \div (x^3)^3 = x^3$

⑤ $4x^3y \times (-3x^2y)^2 = 36x^7y^3$

해설

③ $3(ab^2c^4)^2 = 3a^2b^4c^8$

39. $\left(-\frac{3xy^2}{x}\right)^3 \times \frac{xz^2}{3y} \div \left(\frac{xy}{z}\right)^2$ 을 간단히 하면?

① $\frac{9z}{x}$ ② $-\frac{9y^3z^4}{x}$ ③ $\frac{3z^2}{y}$
④ $\frac{27xy}{z}$ ⑤ $-\frac{3yz}{x^2}$

해설

$$(\text{준식}) = -\frac{27x^3y^6}{x^3} \times \frac{xz^2}{3y} \times \frac{z^2}{x^2y^2} = -\frac{9y^3z^4}{x}$$

40. $4xy \div (x^2y) \times \left(\frac{xy}{2}\right)^2$ 을 계산하면?

- ① $\frac{16}{x^3y^2}$ ② $\frac{8}{x^3y^2}$ ③ $2xy^2$ ④ xy^2 ⑤ x^2y^2

해설

$$4xy \times \frac{1}{x^2y} \times \frac{x^2y^2}{4} = xy^2$$

41. $(4x^3y)^2 \div (-2xy)^2 \div 4x^3y^2$ 을 간단히 한 것은?

① $\frac{x}{y^2}$

④ $2x^2y$

② $2xy^2$

⑤ $-2xy$

③ $-2x^2y$

(4x³y)² ÷ (-2xy)² ÷ 4x³y²

= 16x⁶y² × $\left(\frac{1}{4x^2y^2}\right)$ × $\left(\frac{1}{4x^3y^2}\right)$

= $\frac{x}{y^2}$

42. $20x^4y^2 \times (x^3)^2 \div \left(-\frac{2x^5}{y}\right)^2$ 을 간단히 하면?

- ① $-2x^2$ ② $\frac{2x}{y}$ ③ $8x^2$ ④ $20xy^2$ ⑤ $5y^4$

해설

$$(\text{준식}) = 20x^4y^2 \times x^6 \times \frac{y^2}{4x^{10}} = 5y^4$$

43. $(a^2b^4)^3 \times a^3b^2 \div (ab^3)^2$ 을 간단히 하면?

① a^6b^{10}

② $\textcircled{2} a^7b^8$

③ $a^{10}b^{16}$

④ $a^{11}b^5$

⑤ $a^{15}b^8$

해설

$$a^6b^{12} \times a^3b^2 \div a^2b^6 = a^7b^8$$

44. 다음 식을 간단히 하면?

$$(ab^2)^2 \times a^2b \div (ab)^2$$

- ① ab^2 ② ab^3 ③ a^2b^2 ④ a^2b^3 ⑤ a^3b^3

해설

$$(ab^2)^2 \times a^2b \div (ab)^2 = a^2b^4 \times a^2b \times \frac{1}{a^2b^2} = a^2b^3$$

45. 다음 식을 계산하면?

$$\frac{3}{7}x^4 \times \frac{7}{12}x^3y \div \left(-\frac{1}{4}xy^2\right)$$

- Ⓐ $-\frac{x^6}{y}$ Ⓛ $-\frac{x^4}{y^2}$ Ⓜ $\frac{x^4}{y^2}$ Ⓞ $\frac{x^6}{y}$ Ⓟ $\frac{x^6}{y^2}$

해설

$$\begin{aligned}& \frac{3}{7}x^4 \times \frac{7}{12}x^3y \div \left(-\frac{1}{4}xy^2\right) \\&= \frac{3}{7}x^4 \times \frac{7}{12}x^3y \times \left(-\frac{4}{xy^2}\right) \\&= -\frac{x^6}{y}\end{aligned}$$

46. $\left(\frac{2y}{x}\right)^2 \times x^2y \div \left(-\frac{3}{x}\right) = ax^b y^c$ (a, b, c 는 상수) 일 때, abc 의 값은?

- ① $-\frac{2}{3}$ ② -4 ③ 0 ④ $\frac{8}{3}$ ⑤ 4

해설

$$\frac{4y^2}{x^2} \times x^2y \times \left(-\frac{x}{3}\right) = -\frac{4}{3}xy^3 = ax^b y^c$$

$$\therefore a = -\frac{4}{3}, b = 1, c = 3$$

$$\therefore abc = -4$$

47. 다음 중 옳은 것은?

$$\begin{array}{ll} \textcircled{1} \quad a \div (b \times c) = \frac{ab}{c} & \textcircled{2} \quad a \times (b \div c) = \frac{a}{bc} \\ \textcircled{3} \quad a \div b \times c = \frac{b}{ac} & \textcircled{4} \quad a \div (b \div c) = \frac{ac}{b} \\ \textcircled{5} \quad a \div b \div c = \frac{ac}{b} & \end{array}$$

해설

$$\begin{array}{l} \textcircled{1} \quad a \div (b \times c) = a \div bc = \frac{a}{bc} \\ \textcircled{2} \quad a \times (b \div c) = a \times \frac{b}{c} = \frac{ab}{c} \\ \textcircled{3} \quad a \div b \times c = \frac{a}{b} \times c = \frac{ac}{b} \\ \textcircled{4} \quad a \div (b \div c) = a \div \frac{b}{c} = a \times \frac{c}{b} = \frac{ac}{b} \\ \textcircled{5} \quad a \div b \div c = \frac{a}{b} \times \frac{1}{c} = \frac{a}{bc} \end{array}$$

48. $-2a^2b \times (3ab)^2 \div (-2ab^2)^2 \div 9a^2b^2$ 을 간단히 하면?

① $-a^3b^2$

④ $\frac{a}{b^4}$

② $-\frac{a}{b^2}$

⑤ $\frac{b^2}{a^3}$

③ $-\frac{1}{2b^3}$

해설

$$\begin{aligned} & -2a^2b \times (3ab)^2 \div (-2ab^2)^2 \div 9a^2b^2 \\ &= -2a^2b \times 9a^2b^2 \times \frac{1}{4a^2b^4} \times \frac{1}{9a^2b^2} \\ &= -\frac{1}{2b^3} \text{ } \circ\text{이다.} \end{aligned}$$

49. 다음 식을 간단히 한 것으로 옳은 것은?

$$3x^2y^3 \times (x^2)^2 \div (-2y^2)^3$$

- ① $-\frac{2x^6}{4y^3}$ ② $-\frac{3x^5}{4y^3}$ ③ $-\frac{3x^6}{8y^3}$ ④ $\frac{3x^5}{8y^3}$ ⑤ $-\frac{3x^5}{8y^3}$

해설

$$\begin{aligned} 3x^2y^3 \times (x^2)^2 \div (-2y^2)^3 &= 3x^2y^3 \times x^4 \times \frac{1}{-8y^6} \\ &= -\frac{3x^6}{8y^3} \end{aligned}$$

이므로 ③ 이다.

50. 다음 중 계산 결과가 옳지 않은 것은?

- ① $(-2xy^2) \times (3x)^2 \div (6y)^2 = -\frac{x^3}{2}$
- ② $14a^2 \div (-2b^2)^2 \times (2ab^2)^2 = 14a^4$
- ③ $\left(\frac{2}{3}a^2\right)^2 \times (3b^2)^2 \div (4ab^2)^2 = \frac{a^2}{4}$
- ④ $(10a)^2 \times (-ab^2)^2 \div \left(-\frac{1}{3}ab^2\right)^2 = 25a^2$
- ⑤ $(-4x^2y) \div \left(-\frac{2}{3}y^2\right) \times (2xy^2)^3 = 48x^5y^5$

해설

① $(-2xy^2) \times 9x^2 \times \frac{1}{36y^2} = -\frac{x^3}{2}$

② $14a^2 \div 4b^4 \times 4a^2b^4 = 14a^4$

③ $\frac{4}{9}a^4 \times 9b^4 \times \frac{1}{16a^2b^4} = \frac{a^2}{4}$

④ $(10a)^2 \times (-ab^2)^2 \div \left(-\frac{1}{3}ab^2\right)^2$
 $= 100a^2 \times a^2b^4 \div \frac{1}{9}a^2b^4 = 900a^2$

⑤ $(-4x^2y) \times \left(-\frac{3}{2}y^2\right) \times 8x^3y^6 = 48x^5y^5$

51. $-3x^2y \div (2xy^a)^2 \times \left(\frac{xy}{3}\right)^b = -\frac{x^2}{12y}$ 일 때, $a+b$ 의 값은?

- ① 2 ② 4 ③ 6 ④ 8 ⑤ 10

해설

$$\begin{aligned} (\text{준식}) &= -3x^2y \div 4x^2y^{2a} \times \frac{x^b y^b}{3^b} \\ &= -3^{1-b} \cdot 4^{-1} x^{2-2+b} \cdot y^{1-2a+b} \\ &= -\frac{x^2}{12y} \\ &= -4^{-1} \cdot 3^{-1} x^2 y^{-1} \end{aligned}$$

$$\therefore 1-b = -1$$

$$b=2$$

$$1-2a+b = 1-2a+2 = -1$$

$$a=2$$

$$\therefore a+b=4$$

52. $x = 3, y = -2, z = 6$ 일 때, $xy^4z \times (-2x^2y)^3 \div (2x^3y^3z)^2$ 의 값은?

- ① -6 ② -4 ③ -2 ④ 2 ⑤ 4

해설

$$(\text{준식}) = xy^4z \times (-8x^6y^3) \times \frac{1}{4x^6y^6z^2} = -\frac{2xy}{z}$$

$$\text{식의 값} : -\frac{2 \times 3 \times (-2)}{6} = 2$$

53. $(-ab^3)^2 \times \left(\frac{a^3}{b}\right)^2 \div \{-(a^2b)^2\}$ 을 간단히 하면?

① a^3b^2

④ $\frac{a^3}{b^2}$

② $-a^4b^2$

⑤ $-\frac{a^3}{b^2}$

③ $-a^2b^3$

해설

$$(\text{준식}) = a^2b^6 \times \frac{a^6}{b^2} \times \left(-\frac{1}{a^4b^2}\right)$$

$$= -a^4b^2$$

54. $-3x^2y \div (2xy^a)^2 \times \left(\frac{xy}{3}\right)^b = -\frac{x^2}{12y}$ 일 때, $a+b$ 의 값은?

- ① 2 ② 4 ③ 6 ④ 8 ⑤ 10

해설

$$-3x^2y \times \frac{1}{4x^2y^{2a}} \times \frac{x^b y^b}{3^b} = -\frac{x^2}{12y}$$

$$-\frac{x^b}{4 \times 3^{b-1} y^{2a-1-b}} = -\frac{x^2}{12y}$$

$$b = 2, 2a - 1 - b = 1 \quad \therefore a = 2$$

$$\therefore a + b = 4$$

55. $x = 3, y = -2, z = -12$ 일 때, $xy^4z \times (-2x^2y)^3 \div (2x^3y^3z)^2$ 의 값은?

- ① -5 ② -4 ③ -1 ④ 1 ⑤ 3

해설

$$(\text{준식}) = xy^4z \times (-8x^6y^3) \times \frac{1}{4x^6y^6z^2} = -\frac{2xy}{z}$$

$$\text{식의 값} : -\frac{2 \times 3 \times (-2)}{-12} = -1$$

56. $(3x - 4) + (x + 3)$ 을 간단히 하면?

- ① $3x + 3$ ② $3x - 1$ ③ $4x - 4$
④ $4x - 1$ ⑤ $4x - 3$

해설

$$\begin{aligned}(3x - 4) + (x + 3) &= 3x - 4 + x + 3 \\&= 4x - 1\end{aligned}$$

57. $(3a + b) + (2a - 3b)$ 를 간단히 하면?

- ① $5a + 4b$ ② $\textcircled{2} 5a - 2b$ ③ $5a - 4b$
④ $-5a - 2b$ ⑤ $-5a + 4b$

해설

$$\begin{aligned}(3a + b) + (2a - 3b) &= 3a + b + 2a - 3b \\&= 5a - 2b\end{aligned}$$

58. $(\quad) - (5x - 2y) = 2x + y$ 에서 (\quad) 안에 알맞은 식은?

- ① $-3x - y$ ② $-3x + y$ ③ $-3x - 2y$
④ $\textcircled{7}x - y$ ⑤ $7x + 2y$

해설

$$\begin{aligned} (\quad) &= (2x + y) + (5x - 2y) \\ &= 2x + y + 5x - 2y \\ &= 7x - y \end{aligned}$$

59. $(\quad) - (5x - 6y) = -3x - y$ 에서 (\quad) 안에 알맞은 식은?

- ① $2x - 3y$ ② $2x - 5y$ ③ $\textcircled{2} 2x - 7y$
④ $5x - 2y$ ⑤ $5x - 5y$

해설

$$\begin{aligned} (\quad) &= (-3x - y) + (5x - 6y) \\ &= -3x - y + 5x - 6y \\ &= 2x - 7y \end{aligned}$$

60. $(3x - 4y - 3) + (x - 2y - 3)$ 을 간단히 하면?

- ① $2x - 3y + 6$ ② $2x - 2y + 4$ ③ $4x - 4y - 6$
④ $4x - 6y - 6$ ⑤ $4x - 6y + 6$

해설

$$\begin{aligned}(3x - 4y - 3) + (x - 2y - 3) \\= 3x - 4y - 3 + x - 2y - 3 \\= 4x - 6y - 6\end{aligned}$$

61. $(5x - y + 3) + (3x + 2y - 4) = ax + by + c$ 일 때, $a + b + c$ 의 값은?

- ① -4 ② -2 ③ 4 ④ 6 ⑤ 8

해설

$$\begin{aligned}(5x - y + 3) + (3x + 2y - 4) \\= 5x - y + 3 + 3x + 2y - 4 \\= 8x + y - 1\end{aligned}$$

따라서 $a = 8, b = 1, c = -1$ 이므로

$a + b + c = 8$ 이다.

62. $\left(\frac{4}{3}x + \frac{5}{12}y - \frac{7}{4}\right) + \left(-\frac{1}{4}x - \frac{7}{6}y + \frac{2}{3}\right)$ 를 간단히 했을 때, x 의 계수와 상수항의 합은?

- ① -3 ② $-\frac{11}{4}$ ③ $-\frac{4}{3}$ ④ 0 ⑤ 1

해설

$$\begin{aligned}& \left(\frac{4}{3}x + \frac{5}{12}y - \frac{7}{4}\right) + \left(-\frac{1}{4}x - \frac{7}{6}y + \frac{2}{3}\right) \\&= \left(\frac{16}{12}x + \frac{5}{12}y - \frac{21}{12}\right) + \left(-\frac{3}{12}x - \frac{14}{12}y + \frac{8}{12}\right) \\&= \left(\frac{16x + 5y - 21 - 3x - 14y + 8}{12}\right) \\&= \frac{13x - 9y - 13}{12} \\&= \frac{13}{12}x - \frac{9}{12}y - \frac{13}{12} \\&x \text{ 의 계수 : } \frac{13}{12}, \text{ 상수항 : } -\frac{13}{12} \\&\therefore \frac{13}{12} + \left(-\frac{13}{12}\right) = 0\end{aligned}$$

63. $\left(-\frac{1}{6}x + \frac{4}{3}y - \frac{5}{4}\right) + \left(\frac{3}{2}x + \frac{5}{3}y - \frac{7}{6}\right)$ 을 간단히 했을 때, x 의 계수와 y 의 계수의 합은?

- ① $-\frac{11}{3}$ ② $-\frac{4}{3}$ ③ $\frac{4}{3}$ ④ $\frac{11}{3}$ ⑤ $\frac{13}{3}$

해설

$$\begin{aligned}& \left(-\frac{1}{6}x + \frac{4}{3}y - \frac{5}{4}\right) + \left(\frac{3}{2}x + \frac{5}{3}y - \frac{7}{6}\right) \\&= \left(-\frac{2}{12}x + \frac{16}{12}y - \frac{15}{12}\right) + \left(\frac{18}{12}x + \frac{20}{12}y - \frac{14}{12}\right) \\&= \left(\frac{-2x + 16y - 15 + 18x + 20y - 14}{12}\right) \\&= \frac{16x + 36y - 29}{12} \\&= \frac{16}{12}x + \frac{36}{12}y - \frac{29}{12}\end{aligned}$$

x 의 계수 : $\frac{4}{3}$, y 의 계수 : 3

$$\therefore \frac{4}{3} + 3 = \frac{13}{3}$$

64. 다항식 A 에서 $-x - 2y + 4$ 를 빼었더니 $4x + y - 3$ 이 되었다. 이때, 다항식 A 는?

- ① $-5x - 3y - 7$ ② $-5x - y + 1$ ③ $3x - y + 1$
④ $5x + 3y - 7$ ⑤ $5x + 3y + 7$

해설

$$\begin{aligned} A &= (4x + y - 3) + (-x - 2y + 4) \\ &= 4x + y - 3 - x - 2y + 4 \\ &= 3x - y + 1 \end{aligned}$$

65. 다항식 A 에서 $-2x + 3y + 1$ 를 빼었더니 $3x + 2y - 3$ 이 되었다. 이때, 다항식 A 는?

- ① $-x - 3y - 5$ ② $-x - y + 1$ ③ $x + 5y - 2$
④ $5x + 3y + 1$ ⑤ $5x + 2y - 3$

해설

$$\begin{aligned} A &= (3x + 2y - 3) + (-2x + 3y + 1) \\ &= 3x + 2y - 3 - 2x + 3y + 1 \\ &= x + 5y - 2 \end{aligned}$$