

1. $\sqrt{12} \times \sqrt{15} \times \sqrt{35} = a\sqrt{7}$ 일 때, a 의 값은?

① 15

② 20

③ 25

④ 30

⑤ 35

해설

$$\begin{aligned} & \sqrt{12} \times \sqrt{15} \times \sqrt{35} \\ &= \sqrt{2^2 \times 3} \times \sqrt{3 \times 5} \times \sqrt{5 \times 7} \\ &= 30\sqrt{7} \end{aligned}$$

2. $\sqrt{72} = a\sqrt{2}$, $\sqrt{300} = b\sqrt{3}$ 일 때, $a - b$ 의 값은?

① -2

② -4

③ 4

④ 6

⑤ 8

해설

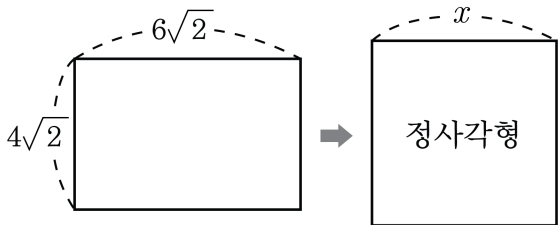
$$\sqrt{72} = \sqrt{2^2 \times 3^2 \times 2} = 6\sqrt{2}$$

$$\sqrt{300} = \sqrt{10^2 \times 3} = 10\sqrt{3}$$

$$\therefore a = 6, b = 10$$

$$\therefore a - b = -4$$

3. 가로 길이가 $6\sqrt{2}$ 이고, 세로 길이가 $4\sqrt{2}$ 인 직사각형과 넓이가 같은 정사각형의 한 변의 길이 x 를 $a\sqrt{b}$ 의 꼴로 나타내면? (단, b 는 제공인 인수가 없는 자연수)



① $2\sqrt{3}$

② $3\sqrt{3}$

③ $4\sqrt{3}$

④ $5\sqrt{3}$

⑤ $6\sqrt{3}$

해설

직사각형의 넓이는 $6\sqrt{2} \times 4\sqrt{2} = 48$ 이다.

따라서 $x^2 = 48$ 이므로 정사각형의 한 변의 길이는 $\sqrt{48} = 4\sqrt{3}$ 이다.

4. $\sqrt{99} \sqrt{715} = A \sqrt{65}$, $6 \sqrt{5} = \sqrt{B}$ 일 때, $B - A$ 의 값을 구하면?

① 144

② 145

③ 146

④ 147

⑤ 148

해설

$$\begin{aligned}\sqrt{99} \sqrt{715} &= \sqrt{3^2 \times 11} \sqrt{5 \times 11 \times 13} \\ &= \sqrt{3^2 \times 5 \times 11^2 \times 13} = 33 \sqrt{65}\end{aligned}$$

$$\therefore A = 33$$

$$6 \sqrt{5} = \sqrt{6^2 \times 5} = \sqrt{180}$$

$$\therefore B = 180$$

$$\therefore B - A = 180 - 33 = 147$$

5. 다음을 만족하는 유리수 a, b, c 에 대하여 $\sqrt{\frac{2ab}{c}}$ 의 값은?

$$\frac{1}{2}\sqrt{8} = \sqrt{a}, \quad \sqrt{135} = 3\sqrt{b}, \quad \sqrt{2000} = c\sqrt{5}$$

① $\sqrt{2}$

② $\sqrt{3}$

③ 2

④ $\sqrt{5}$

⑤ $\sqrt{6}$

해설

$$\frac{1}{2}\sqrt{8} = \sqrt{\left(\frac{1}{2}\right)^2 \times 8} = \sqrt{\frac{8}{4}} = \sqrt{2} = \sqrt{a}$$

$$\therefore a = 2$$

$$\sqrt{135} = \sqrt{3^3 \times 5} = 3\sqrt{15} = 3\sqrt{b}$$

$$\therefore b = 15$$

$$\sqrt{2000} = \sqrt{20^2 \times 5} = 20\sqrt{5} = c\sqrt{5}$$

$$\therefore c = 20$$

$$\therefore \sqrt{\frac{2ab}{c}} = \sqrt{\frac{2 \times 2 \times 15}{20}} = \sqrt{3}$$

6. 다음 수를 근호 안의 수가 가장 작은 자연수가 되도록 $a\sqrt{b}$ 의 꼴로 나타낸 것 중 틀린 것은?

$$\textcircled{1} \quad \sqrt{\frac{27}{121}} = \frac{3\sqrt{3}}{11}$$

$$\textcircled{2} \quad \sqrt{0.005} = \frac{\sqrt{2}}{20}$$

$$\textcircled{3} \quad \sqrt{0.12} = \frac{\sqrt{3}}{3}$$

$$\textcircled{4} \quad \sqrt{\frac{2}{49}} = \frac{\sqrt{2}}{7}$$

$$\textcircled{5} \quad \sqrt{\frac{12}{32}} = \frac{\sqrt{6}}{4}$$

해설

$$\textcircled{1} \quad \sqrt{\frac{27}{121}} = \sqrt{\frac{3^3 \times 3}{11^2}} = \frac{3\sqrt{3}}{11}$$

$$\begin{aligned} \textcircled{2} \quad \sqrt{0.005} &= \sqrt{\frac{50}{10000}} = \sqrt{\frac{5^2 \times 2}{100^2}} \\ &= \frac{5\sqrt{2}}{100} = \frac{\sqrt{2}}{20} \end{aligned}$$

$$\textcircled{3} \quad \sqrt{0.12} = \sqrt{\frac{12}{100}} = \frac{\sqrt{12}}{10} = \frac{1}{10} \times 2\sqrt{3} = \frac{\sqrt{3}}{5}$$

$$\textcircled{4} \quad \sqrt{\frac{2}{49}} = \sqrt{\frac{2}{7^2}} = \frac{\sqrt{2}}{7}$$

$$\textcircled{5} \quad \sqrt{\frac{12}{32}} = \sqrt{\frac{6}{16}} = \frac{\sqrt{6}}{4}$$

7. $\sqrt{1.92} = a\sqrt{3}$, $\sqrt{\frac{63}{64}} = b\sqrt{7}$ 일 때, 유리수 a, b 에 대하여 ab 의 값을 구하면?

- ① 0.3 ② 0.5 ③ 1 ④ 1.5 ⑤ 3

해설

$$\sqrt{1.92} = \sqrt{\frac{192}{100}} = \sqrt{\frac{8^2 \times 3}{10^2}} = \frac{8\sqrt{3}}{10} = \frac{4}{5}\sqrt{3}$$

$$\therefore a = \frac{4}{5}$$

$$\sqrt{\frac{63}{64}} = \sqrt{\frac{3^2 \times 7}{8^2}} = \frac{3\sqrt{7}}{8}$$

$$\therefore b = \frac{3}{8}$$

$$\therefore ab = \frac{4}{5} \times \frac{3}{8} = \frac{3}{10} = 0.3$$

8. 다음 보기의 네 개의 수를 작은 순서부터 나열할 때, 바르게 나타낸 것은?

보기

$$\textcircled{㉠} \sqrt{0.28}$$

$$\textcircled{㉡} \frac{\sqrt{7}}{2}$$

$$\textcircled{㉢} \sqrt{\frac{14}{18}}$$

$$\textcircled{㉣} \sqrt{\frac{7}{169}}$$

$$\textcircled{1} \textcircled{㉣} < \textcircled{㉢} < \textcircled{㉡} < \textcircled{㉠}$$

$$\textcircled{2} \textcircled{㉡} < \textcircled{㉠} < \textcircled{㉢} < \textcircled{㉣}$$

$$\textcircled{3} \textcircled{㉣} < \textcircled{㉠} < \textcircled{㉡} < \textcircled{㉢}$$

$$\textcircled{4} \textcircled{㉢} < \textcircled{㉣} < \textcircled{㉠} < \textcircled{㉡}$$

$$\textcircled{5} \textcircled{㉡} < \textcircled{㉢} < \textcircled{㉠} < \textcircled{㉣}$$

해설

$$\textcircled{㉠} \sqrt{0.28} = \sqrt{\frac{28}{100}} = \sqrt{\frac{7}{25}} = \frac{\sqrt{7}}{5}$$

$$\textcircled{㉡} \frac{\sqrt{7}}{2}$$

$$\textcircled{㉢} \sqrt{\frac{14}{18}} = \sqrt{\frac{7}{9}} = \frac{\sqrt{7}}{3}$$

$$\textcircled{㉣} \sqrt{\frac{7}{169}} = \sqrt{\frac{7}{13^2}} = \frac{\sqrt{7}}{13}$$

$$\therefore \textcircled{㉣} < \textcircled{㉠} < \textcircled{㉢} < \textcircled{㉡}$$

9. $\sqrt{0.96}$ 은 $\sqrt{6}$ 의 x 배이다. 이 때, x 의 값은?

① $\frac{1}{5}$

② $\frac{2}{5}$

③ $\frac{8}{5}$

④ $\frac{12}{5}$

⑤ $\frac{16}{5}$

해설

$$\sqrt{0.96} = \sqrt{\frac{96}{100}} = \sqrt{\frac{4^2 \times 6}{10^2}} = \frac{4}{10} \sqrt{6} = \frac{2}{5} \sqrt{6}$$

$$\therefore x = \frac{2}{5}$$

10. 분모를 유리화한다고 할 때, $\frac{\sqrt{6}}{\sqrt{45}} = \frac{\sqrt{6} \times \square}{3 \times \square \times \square}$ 에서, $\square$ 안에 공통으로 들어갈 수는?

① $\sqrt{2}$

② $\sqrt{3}$

③ $\sqrt{5}$

④ $\sqrt{6}$

⑤ $\sqrt{15}$

해설

$$\frac{\sqrt{6}}{\sqrt{45}} = \frac{\sqrt{6}}{3\sqrt{5}} = \frac{\sqrt{6} \times \sqrt{5}}{3\sqrt{5} \times \sqrt{5}} = \frac{\sqrt{30}}{15}$$

$$\therefore \square = \sqrt{5}$$

11. 분수 $\frac{3\sqrt{10} - \sqrt{18}}{\sqrt{5}}$ 의 분모를 유리화하면?

① $\frac{10\sqrt{2} - 3\sqrt{10}}{5}$

② $\frac{10\sqrt{2} + 3\sqrt{10}}{5}$

③ $\frac{15\sqrt{2} - 3\sqrt{10}}{5}$

④ $\frac{15\sqrt{2} + 3\sqrt{10}}{5}$

⑤ $\frac{-15\sqrt{2} + 3\sqrt{10}}{5}$

해설

$$(\text{준식}) = \frac{(3\sqrt{10} - \sqrt{18}) \times \sqrt{5}}{\sqrt{5} \times \sqrt{5}} = \frac{15\sqrt{2} - 3\sqrt{10}}{5}$$

12. $\frac{3\sqrt{a-4}}{\sqrt{18}} = 3$ 일 때, a 의 값은?

① 24

② 22

③ 20

④ 18

⑤ 16

해설

$$\frac{3\sqrt{a-4}}{\sqrt{18}} = \frac{3\sqrt{a-4} \times \sqrt{2}}{3\sqrt{2} \times \sqrt{2}} = \frac{\sqrt{a-4} \times \sqrt{2}}{2} = 3$$

$$\sqrt{a-4} \times \sqrt{2} = 6 = \sqrt{36}$$

$$(a-4) \times 2 = 36$$

$$a-4 = 18$$

$$\therefore a = 22$$

13. $x = 3 + \sqrt{2}$ 일 때, $\frac{x+7}{x-3}$ 의 값은?

① $-1 + 5\sqrt{2}$

② $1 - 3\sqrt{2}$

③ $1 + 5\sqrt{2}$

④ $2 + 2\sqrt{2}$

⑤ $2 + 5\sqrt{2}$

해설

$$\frac{x+7}{x-3} = \frac{10+\sqrt{2}}{\sqrt{2}} = \frac{10+\sqrt{2}}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} = 5\sqrt{2} + 1$$

14. $A = 3\sqrt{3} + 7\sqrt{3} - 2\sqrt{3}$, $B = 8\sqrt{6} - 9\sqrt{6} - 14\sqrt{6}$ 일 때, $A + B$ 의 값은?

① $-7\sqrt{3}$

② $-7\sqrt{6}$

③ $-8\sqrt{3} + 15\sqrt{6}$

④ $6\sqrt{3} - 5\sqrt{6}$

⑤ $8\sqrt{3} - 15\sqrt{6}$

해설

$$A = 3\sqrt{3} + 7\sqrt{3} - 2\sqrt{3} = 8\sqrt{3}$$

$$B = 8\sqrt{6} - 9\sqrt{6} - 14\sqrt{6} = -15\sqrt{6}$$

$$\therefore A + B = 8\sqrt{3} - 15\sqrt{6}$$

15. $\frac{\sqrt{3}}{3} + \frac{\sqrt{5}}{6} - \frac{\sqrt{3}}{4} - \frac{\sqrt{5}}{2}$ 을 간단히 나타내면?

① $-\frac{\sqrt{3}}{12} - \frac{\sqrt{5}}{12}$

② $\frac{\sqrt{3}}{12} + \frac{\sqrt{5}}{3}$

③ $\frac{\sqrt{3}}{12} - \frac{\sqrt{5}}{3}$

④ $\frac{\sqrt{3}}{6} - \frac{\sqrt{5}}{6}$

⑤ $\frac{\sqrt{3}}{3} + \frac{\sqrt{5}}{3}$

해설

$$\begin{aligned} & \frac{\sqrt{3}}{3} + \frac{\sqrt{5}}{6} - \frac{\sqrt{3}}{4} - \frac{\sqrt{5}}{2} \\ &= \frac{4\sqrt{3} - 3\sqrt{3}}{12} + \frac{\sqrt{5} - 3\sqrt{5}}{6} \\ &= \frac{\sqrt{3}}{12} - \frac{\sqrt{5}}{3} \end{aligned}$$

16. 다음 식을 간단히 하면?

$$\sqrt{12} + \sqrt{3} - \sqrt{48}$$

① $-\sqrt{3}$

② $\sqrt{3}$

③ $2\sqrt{3}$

④ $-2\sqrt{3}$

⑤ $7\sqrt{3}$

해설

$$\begin{aligned}\sqrt{12} + \sqrt{3} - \sqrt{48} &= 2\sqrt{3} + \sqrt{3} - 4\sqrt{3} \\ &= -\sqrt{3}\end{aligned}$$

17. $\sqrt{48} - 2\sqrt{3} - \frac{3}{\sqrt{27}}$ 을 간단히 하면?

① $-\frac{2}{3}\sqrt{3}$

② $-\frac{3}{4}\sqrt{3}$

③ $\frac{3}{4}\sqrt{3}$

④ $\frac{2}{3}\sqrt{3}$

⑤ $\frac{5}{3}\sqrt{3}$

해설

$$4\sqrt{3} - 2\sqrt{3} - \frac{3}{3\sqrt{3}} = 2\sqrt{3} - \frac{\sqrt{3}}{3} = \frac{5}{3}\sqrt{3}$$

18. $\sqrt{18} + \sqrt{48} - 2\sqrt{27} + 3\sqrt{50}$ 을 간단히 하면?

① $14\sqrt{2} + 4\sqrt{3}$

② $14\sqrt{2} - 4\sqrt{3}$

③ $18\sqrt{2} - 2\sqrt{3}$

④ $18\sqrt{2} + 2\sqrt{3}$

⑤ $24\sqrt{2} + 4\sqrt{3}$

해설

$$\begin{aligned} & \sqrt{18} + \sqrt{48} - 2\sqrt{27} + 3\sqrt{50} \\ &= 3\sqrt{2} + 4\sqrt{3} - 6\sqrt{3} + 15\sqrt{2} \\ &= (3\sqrt{2} + 15\sqrt{2}) + (4\sqrt{3} - 6\sqrt{3}) \\ &= 18\sqrt{2} - 2\sqrt{3} \end{aligned}$$

19. $\sqrt{45} + \sqrt{80} - k\sqrt{5} = 0$ 일 때, 유리수 k 의 값은?

① 5

② 6

③ 7

④ 8

⑤ 9

해설

$$3\sqrt{5} + 4\sqrt{5} - k\sqrt{5} = 0$$

$$7\sqrt{5} = k\sqrt{5}$$

$$\therefore k = 7$$

20. $\sqrt{2} = a$, $\sqrt{3} = b$ 라고 할 때, $\sqrt{8} + 2\sqrt{27} + \frac{6}{\sqrt{54}} - \frac{3}{\sqrt{18}}$ 을 a, b 를 이용하여 나타내면?

① $\frac{1}{2}a + 6b + \frac{1}{3}ab$

③ $\frac{5}{2}a + 6b + \frac{1}{3}ab$

⑤ $\frac{3}{2}a + 4b + \frac{1}{3}ab$

② $\frac{3}{2}a + 6b + \frac{1}{3}ab$

④ $\frac{1}{2}a + 4b + \frac{1}{3}ab$

해설

$$\begin{aligned} (\text{준식}) &= 2\sqrt{2} + 6\sqrt{3} + \frac{6}{3\sqrt{6}} - \frac{3}{3\sqrt{2}} \\ &= 2\sqrt{2} + 6\sqrt{3} + \frac{\sqrt{6}}{3} - \frac{\sqrt{2}}{2} \\ &= \frac{3}{2}\sqrt{2} + 6\sqrt{3} + \frac{1}{3}\sqrt{2}\sqrt{3} \\ &= \frac{3}{2}a + 6b + \frac{1}{3}ab \end{aligned}$$

21. $\frac{1}{\sqrt{12}} + \frac{3}{\sqrt{27}} - \sqrt{12} = A\sqrt{3}$ 일 때, 유리수 A 의 값은?

① $\frac{1}{2}$

② $-\frac{1}{2}$

③ $\frac{3}{2}$

④ $-\frac{3}{2}$

⑤ $\frac{1}{3}$

해설

$$\begin{aligned}\frac{\sqrt{3}}{6} + \frac{\sqrt{3}}{3} - 2\sqrt{3} &= \frac{3\sqrt{3}}{6} - \frac{12\sqrt{3}}{6} \\ &= -\frac{9\sqrt{3}}{6} \\ &= -\frac{3\sqrt{3}}{2} \text{ 이다.}\end{aligned}$$

따라서 $A = -\frac{3}{2}$ 이다.

22. $\sqrt{32} - 2\sqrt{24} - \sqrt{2}(1 + 2\sqrt{3})$ 을 간단히 하면?

① $3\sqrt{2} - 6\sqrt{6}$

② $3\sqrt{2} + 2\sqrt{6}$

③ $4\sqrt{2} - \sqrt{6}$

④ $4\sqrt{2} + 3\sqrt{6}$

⑤ $5\sqrt{2} + 3\sqrt{6}$

해설

$$\begin{aligned} & \sqrt{32} - 2\sqrt{24} - \sqrt{2}(1 + 2\sqrt{3}) \\ &= 4\sqrt{2} - 4\sqrt{6} - (\sqrt{2} + 2\sqrt{6}) \\ &= 4\sqrt{2} - 4\sqrt{6} - \sqrt{2} - 2\sqrt{6} \\ &= 3\sqrt{2} - 6\sqrt{6} \end{aligned}$$

23. $A = \sqrt{2} - 5\sqrt{3}$, $B = -3\sqrt{2} - \sqrt{3}$ 일 때, $\sqrt{3}A - \sqrt{2}B$ 의 값은?

① $2\sqrt{6} - 9$

② $2\sqrt{6} + 9$

③ -21

④ $-2\sqrt{6} + 21$

⑤ $2\sqrt{6} - 21$

해설

$$\begin{aligned} & \sqrt{3}A - \sqrt{2}B \\ &= \sqrt{3}(\sqrt{2} - 5\sqrt{3}) - \sqrt{2}(-3\sqrt{2} - \sqrt{3}) \\ &= \sqrt{6} - 15 + 6 + \sqrt{6} \\ &= 2\sqrt{6} - 9 \end{aligned}$$

24. $\sqrt{5} \left(\frac{4\sqrt{5}}{\sqrt{10}} + \frac{5}{\sqrt{9}} \right) + \frac{3+4\sqrt{2}}{\sqrt{5}} = a\sqrt{5} + b\sqrt{10}$ 일 때, $b-a$ 의 값은?
(단, a, b 는 유리수)

① $\frac{1}{3}$

② $\frac{2}{5}$

③ $\frac{7}{15}$

④ $\frac{8}{15}$

⑤ $\frac{3}{5}$

해설

$$\begin{aligned} & \sqrt{5} \left(\frac{4\sqrt{5}}{\sqrt{10}} + \frac{5}{\sqrt{9}} \right) + \frac{3+4\sqrt{2}}{\sqrt{5}} \\ &= 2\sqrt{10} + \frac{5\sqrt{5}}{3} + \frac{3\sqrt{5}+4\sqrt{10}}{5} \\ &= 2\sqrt{10} + \frac{4\sqrt{10}}{5} + \left(\frac{5}{3} + \frac{3}{5} \right) \sqrt{5} \\ &= \frac{14\sqrt{10}}{5} + \frac{34}{15} \sqrt{5} \\ &a = \frac{34}{15}, b = \frac{14}{5} \\ &\therefore b-a = \frac{8}{15} \end{aligned}$$

25. 연립방정식 $\begin{cases} \sqrt{2}x + \sqrt{3}y = 5\sqrt{6} \\ \sqrt{3}x - 2\sqrt{2}y = -2 \end{cases}$ 를 풀면?

① $x = \frac{17}{7}\sqrt{3}, y = \frac{18}{7}\sqrt{2}$

③ $x = \frac{17}{7}\sqrt{2}, y = \frac{18}{7}\sqrt{3}$

⑤ $x = \frac{17}{7}\sqrt{3}, y = \frac{18}{7}\sqrt{3}$

② $x = \frac{18}{7}\sqrt{2}, y = \frac{17}{7}\sqrt{3}$

④ $x = \frac{18}{7}\sqrt{3}, y = \frac{17}{7}\sqrt{2}$

해설

$$\begin{cases} \sqrt{2}x + \sqrt{3}y = 5\sqrt{6} \cdots \textcircled{1} \\ \sqrt{3}x - 2\sqrt{2}y = -2 \cdots \textcircled{2} \end{cases}$$

$\textcircled{1} \times 2\sqrt{2} + \textcircled{2} \times \sqrt{3}$ 을 하면

$$\begin{array}{rcl} 4x + 2\sqrt{6}y & = & 20\sqrt{3} \\ +) 3x - 2\sqrt{6}y & = & -2\sqrt{3} \\ \hline 7x & = & 18\sqrt{3} \end{array}$$

$$\therefore x = \frac{18}{7}\sqrt{3}$$

$\textcircled{2}$ 에 $x = \frac{18}{7}\sqrt{3}$ 을 대입하면

$$\frac{54}{7} - 2\sqrt{2}y = -2, \quad \sqrt{2}y = \frac{34}{7}$$

$$y = \frac{17}{7}\sqrt{2}$$