

1. $0 < a < b$ 인 실수, a, b 에 대하여 다음 중 옳은 것은?

$$\begin{array}{ll} \textcircled{1} \frac{a}{1+a} < \frac{b}{1+b} & \textcircled{2} \frac{a}{1+a} \leq \frac{b}{1+b} \\ \textcircled{3} \frac{a}{1+a} > \frac{b}{1+b} & \textcircled{4} \frac{a}{1+a} \geq \frac{b}{1+b} \\ \textcircled{5} \frac{a}{1+a} = \frac{b}{1+b} & \end{array}$$

해설

$$0 < a < b \text{에서 } \frac{1}{a} > \frac{1}{b} \cdots \textcircled{\textcircled{1}}$$

$\textcircled{\textcircled{1}}$ 의 양변에 1을 더하면

$$\frac{1}{a} + 1 > \frac{1}{b} + 1, \quad \frac{1+a}{a} > \frac{1+b}{b} \cdots \textcircled{\textcircled{2}}$$

따라서 $\textcircled{\textcircled{2}}$ 의 역수를 취하면 $\frac{a}{1+a} < \frac{b}{1+b}$