

stress test

1. $18a^3b^3 \div 3a^2b \times 2b$ 은 다음 중どれ인가?

[배점 2, 하중]

- ① $3ab$ ② $6ab^2$ ③ $12ab^2$
 ④ $3ab^3$ ⑤ $12ab^3$

해설

$$18a^3b^3 \times \frac{1}{3a^2b} \times 2b = 12ab^3$$

2. $a \div (b \times c)$ 은 $b \div c$ 에 대한 정답은?

[배점 2, 하중]

- ① $a \div (b \times c) = \frac{ab}{c}$
 ② $a \times (b \div c) = \frac{ab}{c}$
 ③ $(a \div b) \div c = \frac{ac}{b}$
 ④ $(a \div b) \times c = \frac{bc}{a}$
 ⑤ $a \div (b \div c) = \frac{ab}{c}$

해설

- ① $a \div (b \times c) = \frac{a}{bc}$
 ② $a \times (b \div c) = \frac{a}{bc}$
 ③ $(a \div b) \div c = \frac{a}{bc}$
 ④ $(a \div b) \times c = \frac{ac}{b}$
 ⑤ $a \div (b \div c) = \frac{ac}{b}$

3. $2y^2 - \{-y(y - 4) + 4\}$ 은 y 에 대한 정답은?

[배점 2, 하중]

▶ 답:

▷ 정답: 3

해설

$$(i \propto i) = 2y^2 - (-y^2 + 4y + 4) = 3y^2 - 4y - 4$$

$$\therefore a + b - c = 3 - 4 - (-4) = 3$$

4. $a = \frac{1}{2}, b = -\frac{1}{2}$ 은 $a - [3a - \{a - 2b - (7a - 4b)\}]$ 은 a 에 대한 정답은?

[배점 2, 하중]

▶ 답:

▷ 정답: -5

해설

$$(i \propto i) = a - \{3a - (a - 2b - 7a + 4b)\}$$

$$= a - (3a + 6a - 2b)$$

$$= -8a + 2b$$

$$a = \frac{1}{2}, b = -\frac{1}{2}$$

$$\therefore (i \propto i) = -8a + 2b = -4 - 1 = -5$$

5. $2^7 \times 5^4$ ì ' n 자리ì i i °ì i ¼ ë , n ì ê° i ?
[배점 3, 하상]

① 3 ② 4 ③ 5 ④ 6 ⑤ 7

해설

$$\begin{aligned} 2 \times 5 &= 10 \text{ } \text{ì 'ë - ë} \\ 2^7 \times 5^4 &= 2^3 \times 2^4 \times 5^4 = 2^3 \times 10^4 = 8 \times 10000 \\ \text{ë 'ë ¼ì 5 자리ì i i °ì i 'ë} &\text{ì 'ë} \end{aligned}$$

6. $\frac{2^{15} \times 15^{20}}{45^{10}}$ ì 'ë a 자리ì i i , ê° ? [배점 3, 하상]

① 8 자리 ② 10 자리 ③ 11 자리
④ 12 자리 ⑤ 13 자리

해설

$$\begin{aligned} \frac{2^{15} \times 15^{20}}{45^{10}} &= \frac{2^{15} \times (3 \times 5)^{20}}{(3^2 \times 5)^{10}} \\ &= \frac{2^{15} \times 3^{20} \times 5^{20}}{3^{20} \times 5^{10}} \\ &= 2^{15} \times 5^{10} \\ &= 2^5 \times 2^{10} \times 5^{10} \\ &= 32 \times 10^{10} \end{aligned}$$

ë 'ë ¼ì 12 자리ì i i 'ë

7. $(a^2b - a^2) \div a - 2(ab^2 + 6b^2) \div b$ ë 'í i ë ,
ab ì ê 3 ì 'ë ¼ x , a ì ê 3 ì 'ë ¼ y ë ' ¼ í ë , $3x - y$
ì ê 3 ì 'ë -í ì -ë ¼ . [배점 3, 하상]

▶ 답:

▷ 정답: -2

해설

$$\begin{aligned} (i \text{ } \text{ì ' }) &= ab - a - 2ab - 12b \\ &= -a - ab - 12b \\ \therefore 3x - y &= 3 \times (-1) - (-1) = -2 \end{aligned}$$

8. ë 'ì ì $\frac{1}{4}a(2a - 3)$ ì 'ë 'í ë '?

[배점 3, 하상]

- ① $-\frac{1}{4}a^2 - \frac{3}{4}a$
② $-\frac{1}{4}a^2 - \frac{1}{4}a$
③ $\frac{1}{2}a^2 - \frac{3}{4}a$
④ $\frac{1}{2}a^2 + \frac{3}{4}a$
⑤ $\frac{1}{2}a^2 - \frac{3}{4}$

해설

$$\begin{aligned} \frac{1}{4}a \times 2a + \frac{1}{4}a \times (-3) \\ = \frac{1}{2}a^2 - \frac{3}{4}a \end{aligned}$$

9. i i a, b, c, d ì 'ë i - $(2x - 1)(x^2 - 5x + 3) = ax^3 + bx^2 + cx + d$ ì 'ë , a + b + c + d ì 'ë i ?

[배점 3, 하상]

① -3 ② -1 ③ 0 ④ 1 ⑤ 3

해설

$$\begin{aligned}
 & (2x-1)(x^2 - 5x + 3) \\
 &= 2x^3 - 10x^2 + 6x - x^2 + 5x - 3 \\
 &= 2x^3 - 11x^2 + 11x - 3 \\
 &a = 2, b = -11, c = 11, d = -3 \\
 \therefore & a + b + c + d = -1
 \end{aligned}$$

10. $\boxed{\quad}$ \times $\boxed{\quad}$ \times $\boxed{\quad}$ \times $\boxed{\quad}$ $= -27x^{12}y^6$.

$$(-3x\boxed{\quad}y^2)^3 = -27x^{12}y^6$$

[배점 3, 중하]

▶ 답:

▶ 답:

▷ 정답: 4

▷ 정답: 6

해설

$$\begin{aligned}
 x^{3\times\boxed{\quad}} &= x^{12} \\
 \therefore \boxed{\quad} &= 4 \\
 y^{2\times 3} &= y^{\boxed{\quad}} \\
 \therefore \boxed{\quad} &= 6
 \end{aligned}$$

11. \times $\boxed{\quad}$ \times $\boxed{\quad}$ \times $\boxed{\quad}$ \times $\boxed{\quad}$?

[배점 3, 중하]

① $(-1)^2 \times (-1)^4 = (-1)^8$

② $3^2 \times 3^3 = 3^6$

③ $(-2) \times (-2)^3 = (-2)^4$

④ $\boxed{4^3 \times 4^2 = 4^5}$

⑤ $(-3)^2 \times (-3) = 3^2$

해설

① $(-1)^2 \times (-1)^4 = (-1)^{2+4} = (-1)^6$

② $3^2 \times 3^3 = 3^{2+3} = 3^5$

③ $(-2) \times (-2)^3 = (-2)^{1+3} = (-2)^4$

④ $(-3)^2 \times (-3) = 3^{2+1} = 3^3$

12. \times $\boxed{\quad}$ \times $a^{12} \div a^2 \div a^4 \times a^3 \times a^2 \times a^3 \times a^0 \times a^0 \times a^2 \times a^2$?

[배점 3, 중하]

① $a^{12} \div (a^8 \div a^4)$

② $\boxed{(a^4)^3 \div a^2 \div (a^2)^2}$

③ $\frac{a^{12}}{a^8} \div a^2$

④ $a^{12} \div (a^2 \div a^4)$

⑤ $(a^3)^4 \div a^5 \div a^2$

해설

$a^{12} \div a^2 \div a^4 = a^{12-2-4} = a^6$ \times

① $a^{12} \div (a^8 \div a^4) = a^{12} \div (a^{8-4}) = a^{12} \div a^4 = a^8$

② $(a^4)^3 \div a^2 \div (a^2)^2 = a^{12} \div a^2 \div a^4 = a^{12-2-4} = a^6$

③ $\frac{a^{12}}{a^8} \div a^2 = a^{12-8-2} = a^2$

④ $a^{12} \div (a^2 \div a^4) = a^{12} \div (a^{2-4}) = a^{12} \div a^{-2} = a^{12-(-2)} = a^{14}$

⑤ $(a^3)^4 \div a^5 \div a^2 = a^{12-5-2} = a^5$

13. $\boxed{\quad}$ ì ì ö øì 'ê° ê° ì ¥ ê° ö "í ì ì
êµ-í ì -ë ¼.

$$x + 4y - \{2x - (3y - \boxed{\quad}) + y\} = 5x - (3x + 2y)$$

[배점 3, 중하]

▶ 답:

▷ 정답: $-3x + 9y$

해설

$$\begin{aligned} & x + 4y - \left\{ 2x - (3y - \boxed{\quad} + y) + y \right\} \\ &= x + 4y - (2x - 3y + \boxed{\quad} - y + y) \\ &= x + 4y - (2x - 3y + \boxed{\quad}) \\ &= -x + 7y - \boxed{\quad} \\ & -x + 7y - \boxed{\quad} = 5x - 3x - 2y = 2x - 2y \\ \therefore \boxed{\quad} &= -x + 7y - 2x + 2y = -3x + 9y \end{aligned}$$

14. $(4xy - x^3y - 3xy^2) \div \frac{1}{2}xy$ ö ¥ ¼ ê° ö "í í è , ì ì í - ì
í - í "í è a " è ê³ ì í í @ì êµ-í ì -ë ¼.
[배점 3, 중하]

▶ 답:

▷ 정답: 0

해설

$$\begin{aligned} & (4xy - x^3y - 3xy^2) \div \frac{1}{2}xy \\ &= (4xy - x^3y - 3xy^2) \div \frac{xy}{2} \\ &= (4xy - x^3y - 3xy^2) \times \frac{2}{xy} \\ &= 8 - 2x^2 - 6y \\ x^2 & \text{ì } ê³ ì - 2, y \text{ì } ê³ ì - 6, \text{ì ì í - 8} \\ \text{ì 'ë øì í @ì êµ-í ø@' - 2 - 6 + 8} &= 0 \text{ì 'ë ø.} \end{aligned}$$

15. $5x - 2y = -4x + y - 3$ ì ¼ ê , $5x - 2y + 5$ ö ¥ ¼ x ì
ê' í ì ì ¼ êì è í è 'ì 'ë ¼. [배점 3, 중하]

▶ 답:

▷ 정답: $-x + 3$

해설

$$\begin{aligned} 5x - 2y &= -4x + y - 3 \text{ì } ê^3 \text{í í è@'} \\ 3y &= 9x + 3, y = 3x + 1 \\ 5x - 2y + 5 &= 5x - 2(3x + 1) + 5 \\ &= 5x - 6x - 2 + 5 \\ &= -x + 3 \end{aligned}$$

16. $4x + 3y = 2$ ì ¼ ê , $5(x - 3y) - 2(4x - 3y)$ ö ¥ ¼ x
ì ê' í ì ì ¼ êì è í è 'ì 'ë ¼. [배점 3, 중하]

▶ 답:

▷ 정답: $9x - 6$

해설

$$\begin{aligned} 4x + 3y &= 2 \\ \therefore 3y &= -4x + 2 \\ (í øì) &= 5(x - 2 + 4x) - 2(4x - 2 + 4x) \\ &= 5(5x - 2) - 2(8x - 2) \\ &= 9x - 6 \end{aligned}$$

17. $x = 2^{\frac{1}{4}}$ 은, $(x^x)^{(x^x)} = 2^{\square}$ 은 $\boxed{\quad}$ 이다.
 [배점 4, 중중]

▶ 답:

▷ 정답: 8

해설

$$x = 2^{\frac{1}{4}} \text{은 } \rightarrow x^4 = 2 \Rightarrow x = \sqrt[4]{2}$$

$$(2^2)^{(2^2)} = (2^2)^4 = 2^8$$

$$\therefore \boxed{\square} = 8$$

18. $\frac{2^{15} \times 15^{30}}{45^{15}}$ 은 a 자리에서 몇 자리에서 $a^2 + a + 1$ 인가?
 [배점 4, 중중]

▶ 답:

▷ 정답: 273

해설

$$\frac{2^{15} \times 3^{30} \times 5^{30}}{3^{30} \times 5^{15}} = 2^{15} \times 5^{15} = 10^{15}$$

$$a = 16 \quad \therefore a^2 + a + 1 = 273$$

19. A 는 $-x - 2y + 4$ 의 $\frac{1}{4}$ 배이다.
 $4x + y - 3$ 은 A 에 몇 배인가?
 [배점 4, 중중]

① $-x + 2y - 7$

② $-x + 3y - 3$

③ $5x - 2y + 4$

④ $5x + 3y - 7$

⑤ $5x + 3y + 7$

해설

$$\begin{aligned} A &= (-x - 2y + 4) = 4x + y - 3 \text{은 } \rightarrow A = 4x + y - 3 \\ A &= (4x + y - 3) - (-x - 2y + 4) \\ &= 4x + y - 3 + x + 2y - 4 \\ &= 5x + 3y - 7 \end{aligned}$$

20. $2x - 5y + 3$ 은 $6x - y + 4$ 의 $\frac{1}{4}$ 배인가?
 [배점 4, 중중]

① $-6x + 4y - 2$

② $-4x - 4y - 1$

③ $2x + 9y - 2$

④ $8x - 6y + 7$

⑤ $10x - 11y + 10$

해설

$$A = 6x - y + 4$$

$$A = (6x - y + 4) - (2x - 5y + 3) = 4x + 4y + 1$$

$$\therefore (4x + 4y + 1) - (2x - 5y + 3) = 2x + 9y - 2$$

21. y 는 $3x - 5y$ 의 $\frac{1}{4}$ 배이다.

$$(3x - 5y) : 7 = (x - y) : 2$$

[배점 4, 중중]

▶ 답:

▷ 정답: $y = -\frac{1}{3}x$

해설

$$\begin{aligned} 7(x-y) &= 2(3x-5y) \\ 7x - 7y &= 6x - 10y, \quad 3y = -x \quad \therefore y = -\frac{1}{3}x \end{aligned}$$

22. 1MB $\approx 2^{10}$ Byte 1GB $\approx 2^{10} \times 2^{10} = 2^{20}$ Byte

$1 \text{GB} = 1 \text{Byte} \times 2^3 \text{GB} = PMP \times 32 \text{GB}$

$1 \text{Byte} = 1 \text{PMP} \times 256 \text{Byte}$

[배점 5, 중상]

▶ 답:

▷ 정답: 128개

해설

$$\begin{aligned} 1 \text{GB} &\approx 2^{10} \text{Byte} \approx 2^{10} \text{Byte} \times 32 \text{GB} \approx \\ &(32 \times 2^{10}) \text{GB} \approx 32 \text{GB}. \\ (32 \times 2^{10}) \div 256 &= (32 \times 2^{10}) \div (2^8) = 32 \times 2^2 = \\ 32 \times 4 &= 128 \approx 128 \text{Byte}. \\ 1 \text{Byte} &\approx 1 \text{PMP} \approx 128 \text{Byte} \approx 1 \text{Byte}. \\ \text{Byte} &\approx 1 \text{Byte} \approx 1 \text{Byte}. \end{aligned}$$

23. $(-24xy^2) \div 12xy \times A = -8x^2y, \quad -8x^2y^2 \div B \times$
 $x^2y^3 = 2x^3y$? , $A \times B, A \div B$? \triangle $x * y = (8xy^2 +$
 $4xy^2) \div 2xy, \quad x \triangle y = (12x^2y - 8x^2y) \div 4xy$?

[배점 5, 중상]

① $4x^2, -4xy^4$ ② $-\frac{x}{y^4}, -16x^3y^4$

③ $-16x^3y^4, -\frac{x}{y^4}$ ④ $16x^3y^4, \frac{x}{y^4}$

⑤ $-16x^3y^4, -xy^4$

해설

$$\begin{aligned} \frac{-24xy^2}{12xy} \times A &= -8x^2y \quad \therefore \\ -2y \times A &= -8x^2y \quad \therefore A = 4x^2 \\ \frac{-8x^2y^2 \times x^2y^3}{B} &= 2x^3y \quad \therefore \\ \frac{-8x^4y^5}{B} &= 2x^3y \quad \therefore B = -4xy^4 \\ \therefore A \times B &= 4x^2 \times (-4xy^4) = -16x^3y^4 \\ \therefore A \div B &= 4x^2 \div (-4xy^4) = -\frac{x}{y^4} \end{aligned}$$

24. $\left(\frac{a^3b^\Delta}{a^\Delta b^4}\right)^3 = \frac{b^3}{a^6} \quad \triangle \approx 1/4 \quad \triangle \approx 3$

[배점 5, 중상]

▶ 답:

▷ 정답: 5

해설

$$\begin{aligned} \left(\frac{a^3b^\Delta}{a^\Delta b^4}\right)^3 &= \frac{b^3}{a^6} \\ \text{i) } 9 - 3\Delta &= -6, \quad \Delta = 5 \\ \text{ii) } 3\Delta - 12 &= 3, \quad \Delta = 5 \end{aligned}$$

25. x, y ? , \triangle $x * y = (8xy^2 +$
 $4xy^2) \div 2xy, \quad x \triangle y = (12x^2y - 8x^2y) \div 4xy$?

$\frac{(x * y) - (x \triangle y)}{(x * y) + (x \triangle y)}$?

① $\frac{6y+x}{6y+x}$ ② $\frac{6y-x}{6y-x}$ ③ $\frac{6y-x}{6y+x}$

④ $\frac{6y+x}{6y-x}$ ⑤ $\frac{3y-x}{3y+x}$

해설

$$\begin{aligned}x * y &= (8xy^2 + 4xy^2) \div 2xy = 4y + 2y \\x \triangle y &= (12x^2y - 8x^2y) \div 4xy = 3x - 2x = x \\\therefore \frac{(x * y) - (x \triangle y)}{(x * y) + (x \triangle y)} &= \frac{6y - x}{6y + x}\end{aligned}$$